

*Evolution beam parameters during
injection and storage of the high
brightness beams envisaged for the
Linac4 injection into the CERN PS
Booster*

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Acknowledgements

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S.M. COUSINEAU (ORNL), F.W. JONES (TRIUMF)



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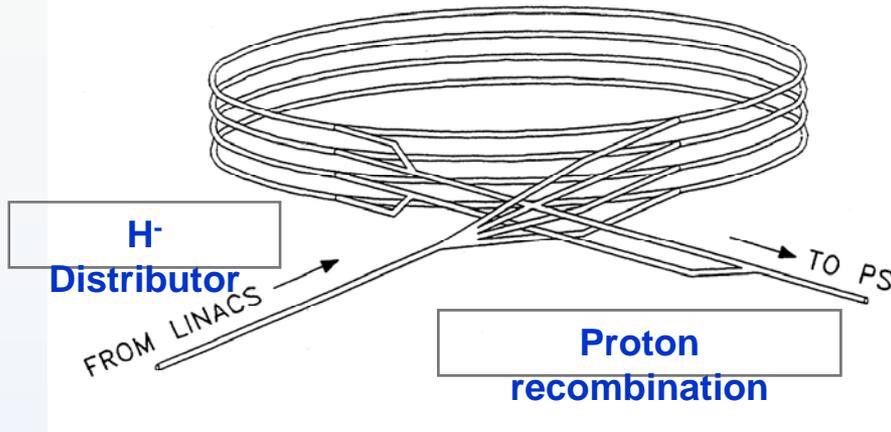
Agenda

- ✓ Studies of the injection and storage of the 160 MeV Linac4 beam for LHC into the CERN PS Booster (PSB)
 - Simulations with the **Orbit** code of the H⁻ charge exchange injection and following beam emittance evolution at 160 MeV
 - Injection done via a painting scheme for optimal shaping of the initial particle distribution
- ✓ Benchmarking of the **Orbit** and **Accsim** simulations with measurements performed in the PSB on the actual high intensity beam stored at 160 MeV

Motivation for the upgrade of the PSB with Linac4:
Deliver beams for the LHC, CNGS and ISOLDE of higher intensity or brightness than presently achieved

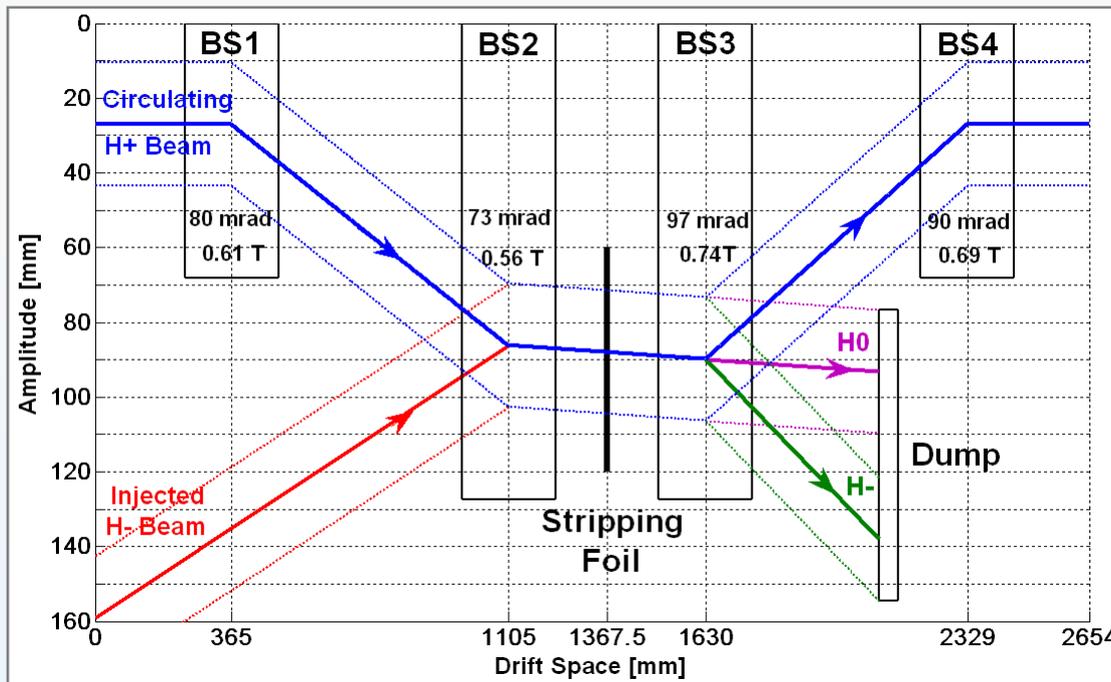
PS Booster overview

FROM CH. CARLI



- ✓ Actual PS Booster (PSB)
 - 4 superimposed rings (16 triplet cells, $\Delta\phi \gtrsim 90^\circ$ per period)
 - Multi-turn injection at 50 MeV with betatron stacking and septum
 - Large acceptances of $A_{H,V} = 180/120 \mu\text{m}$
 - Acceleration to 1400 MeV in ~ 500 ms, double harmonic RF ($h=1$, $h=2$)
 - High space charge regime up to ~ 0.5 tune spreads at 50 MeV
- ✓ Upgrade PS Booster with Linac4 at 160 MeV
 - 10^{14} particles per pulse of 0.4 ms, 1.1 Hz repetition rate
 - Increase of intensity within given normalized emittances by a factor 2
 - Increase of PS Booster injection energy from 50 MeV to 160 MeV
 - $(\beta\gamma^2)_{160\text{MeV}} / (\beta\gamma^2)_{50\text{MeV}} \sim 2$ (space charge decreased by a factor 2 within equal normalized emittance)
 - H⁻ charge exchange injection, Linac4 beam chopping

PSB injection – Hardware layout



W. WETERINGS ET AL.

PSB injection region

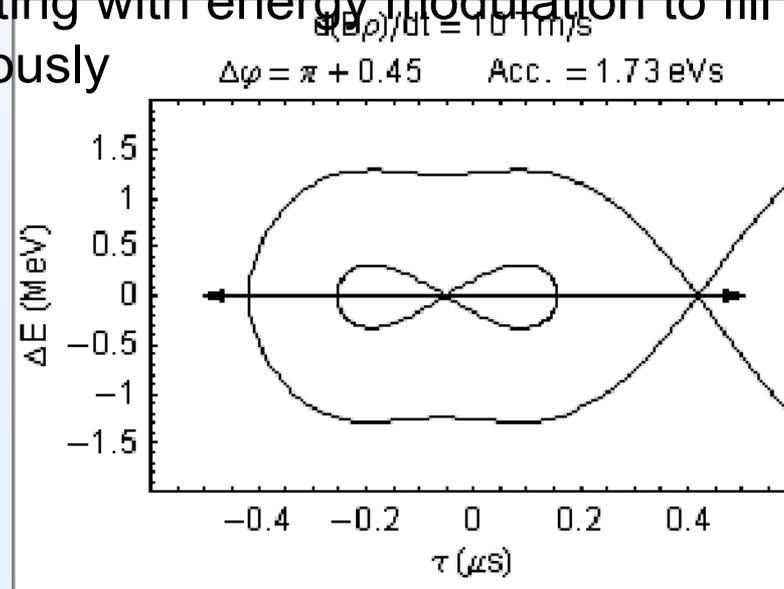
Injected & circulating 1st turn beam envelopes of $\pm 4\sigma$ with partly-stripped H^0 and un-stripped H^-

- ✓ 160 MeV H^- Linac4 beam injection system
 - Two independent closed orbit bump systems
 - Injection “chicane”, 4 pulsed dipole magnets (BS), yielding ~ 61 mm beam offset throughout the injection process
 - Painting bump, 4 horizontal kickers (KSW, outside the injection region), giving a ~ 28 mm closed orbit bump with falling amplitude during the injection for horizontal phase space painting
 - Stripping efficiency of $\sim 98\%$ expected (through a graphite stripping foil)

PSB injection – Longitudinal painting scheme

FROM CH. CARLI

- ✓ PSB with Linac4: similar RF system than at present
 - Double harmonic
 - fundamental $h=1$ & $h=2$, systems to flatten bunches and reduce tune shifts
 - Injection with $\partial(B\rho)/\partial t=10$ Tm/s
 - Little but not negligible motion in longitudinal phase space
 - Active painting with energy modulation to fill bucket homogeneously

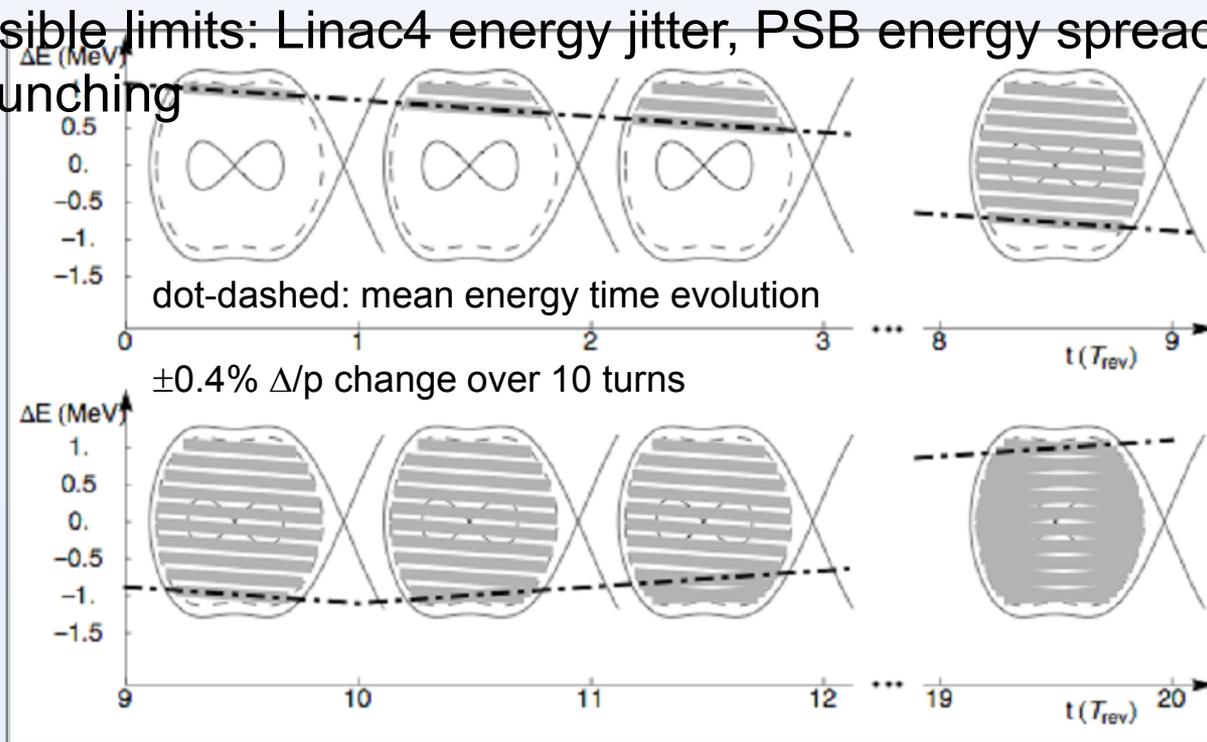


Accelerating RF bucket for a beam in a double harmonic system ($h=1$ & $h=2$)

PSB injection – Longitudinal painting scheme

FROM CH. CARLI

- ✓ Principle of longitudinal painting
 - Triangular Linac4 energy modulation (slow, ~ 20 turns for LHC, ~ 41 mA peak, 3.25×10^{12} p/ring)
 - Beam on if mean energy inside a contour $\sim 80\%$ of acceptance, off if mean energy outside (via a chopper, chopping factor $\sim 62\%$)
 - Higher intensities: several and/or longer modulation periods (~ 41 mA)
 - Possible limits: Linac4 energy jitter, PSB energy spread due to debunching



PSB injection –Painting and tracking with ORBIT

- ✓ Nominal LHC beam with Linac4
 - Single batch PSB transfer: 3 out of 4 rings used, 6 bunches from 3 rings delivered (2 bunches per ring)
 - PSB intensity per ring at 1.4 GeV for loss-free / lossy transmission to LHC: 2.76×10^{12} / 3.25×10^{12} particles
 - Required PSB transverse normalized emittances: $\varepsilon_{H,V}^n(1\sigma) = 2.5 \mu\text{m}$

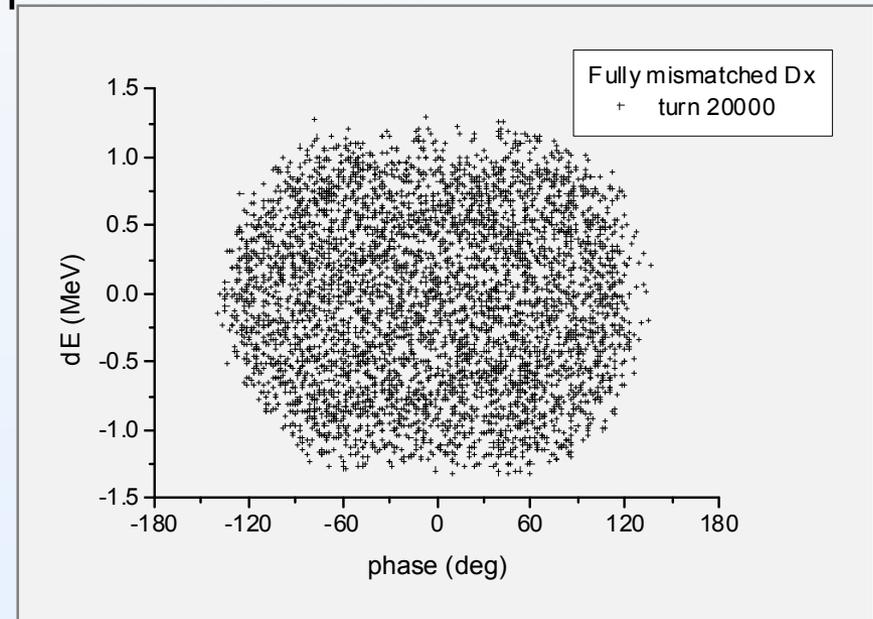
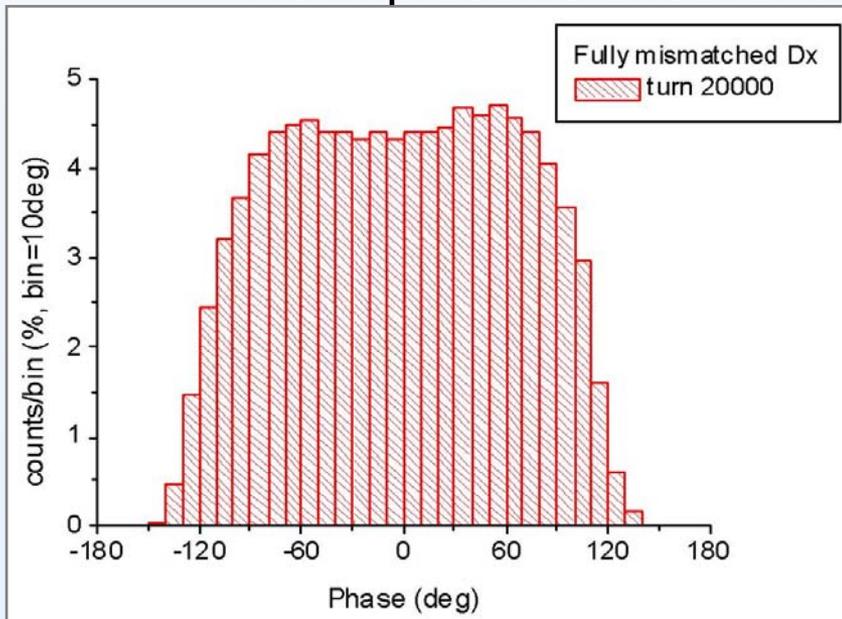
- ✓ ORBIT model (without acceleration)
 - Injection particle distribution
 - 20 beam files (12000 particles per injected turn), containing the 6D particle distributions at the end of the transfer line (**FROM B. GODDARD**)
 - The longitudinal painting process with proper chopping was implemented during the building of the above particle distributions
 - ORBIT simulations
 - The injection “chicane” and transverse painting bumps are implemented (thin lens approximation) (~400 turns BS dipole fall time)
 - Beam files are injected turn by turn (over 20 turns, ~20 μs)
 - Bucket “filling up” via double harmonic RF system: 8 kV (h=1), 6 kV (h=2)
 - Foil heating $\Delta T \sim 500^\circ\text{K}$, ~9.5 foil hits per proton

FROM M. AIBA

PSB injection –Painting and tracking with ORBIT

- ✓ Nominal LHC beam at 160 MeV PSB injection
 - Mismatched dispersion at injection (end line: $D_{\text{Linac4}}=0\text{m}$, $D_{\text{PSB}}\approx-1.4\text{m}$)
 - Bunching factor ~ 0.60
 - No impressive effect of dispersion mismatch

FROM M. AIBA



ORBIT : Longitudinal profile (flat)
(2.2×10^5 macro-particles)

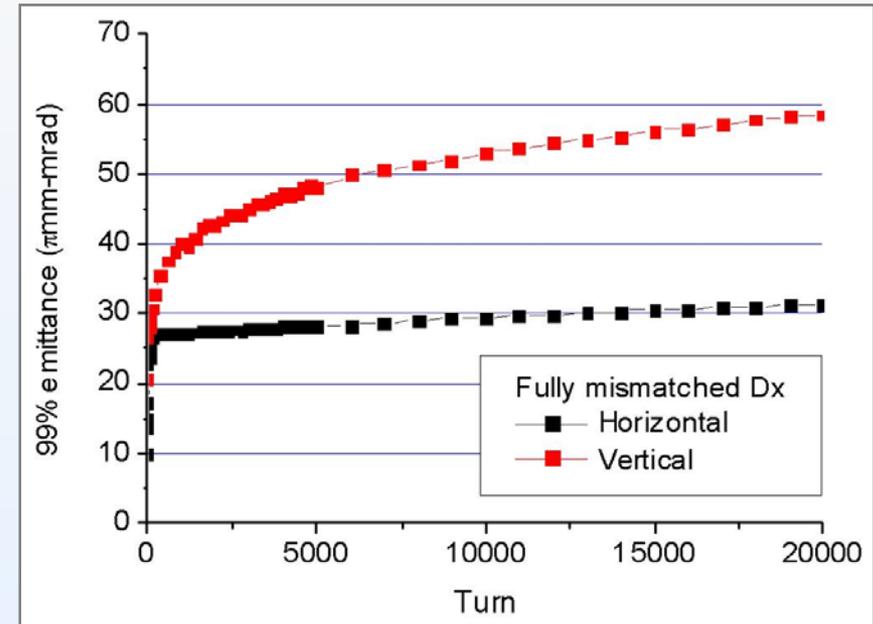
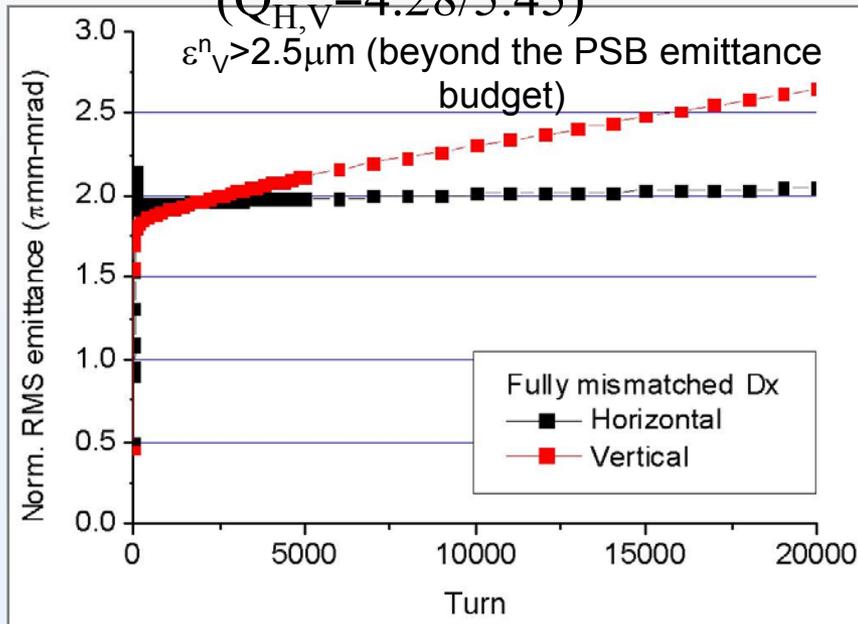
ORBIT : Longitudinal phase-space plot
 ϕ - ΔE [deg-MeV] (2.2×10^5 macro-particles)

PSB injection –Painting and tracking with ORBIT

FROM M. AIBA

- ✓ Emittance evolution on a 160 MeV energy plateau
 - Painting and subsequent tracking up to 2×10^4 turns
 - Simulation done with space charge, $\Delta Q_{H,V} \sim -0.27/-0.32$

($Q_{H,V} = 4.28/5.45$)



ORBIT : Emittances after injection

$\epsilon^n_{H,V}(1\sigma)$ [μm] (2.2×10^5 macro-particles)

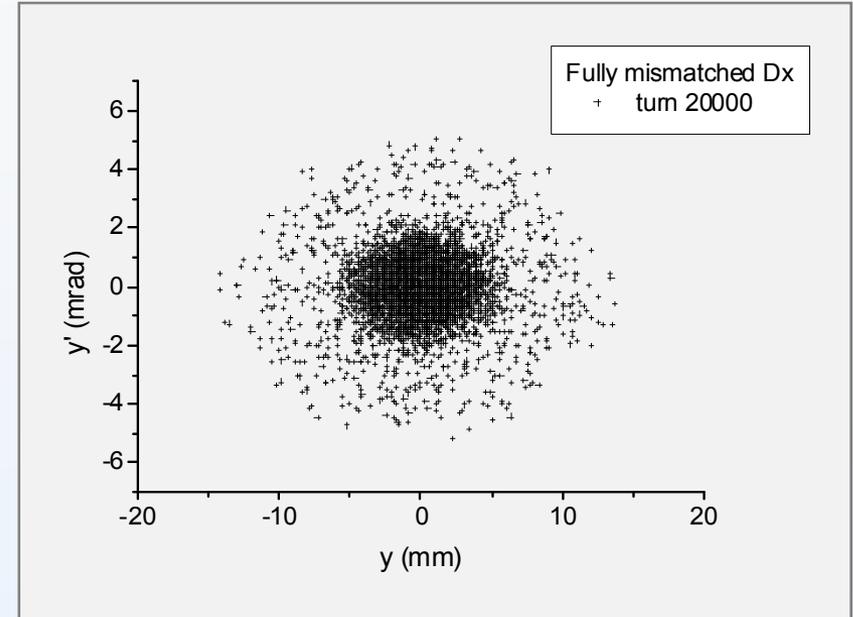
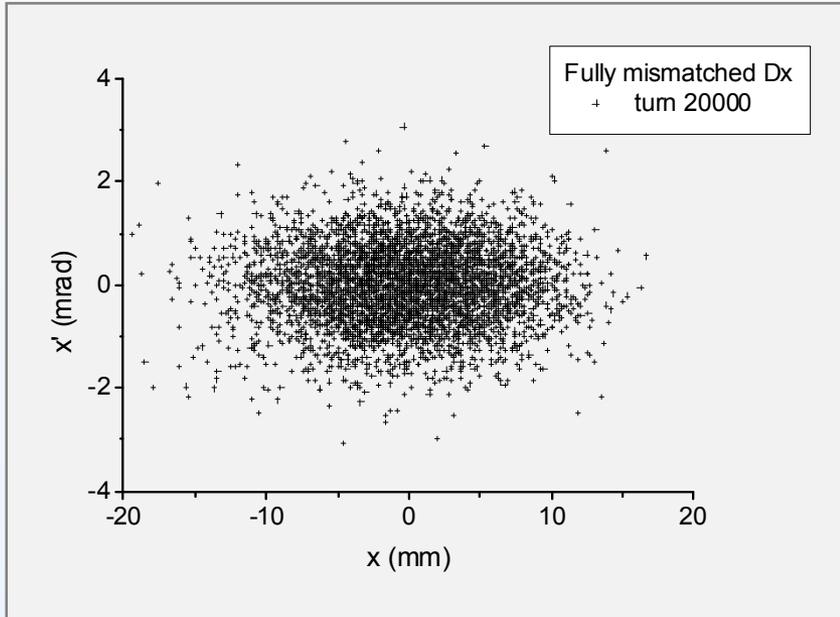
ORBIT : Emittances after injection

$\epsilon^n_{H,V}(99\%)$ [μm] (2.2×10^5 macro-particles)

Remark: **$\sim 8\%$ rms vertical emittance blow-up reduction** after 10^4 turns when using 4 times more macro-particles ($\sim 9 \times 10^5$)

PSB injection –Painting and tracking with ORBIT

FROM M. AIBA



ORBIT : Transverse phase-space scatter plots
 $X-X'$ & $Y-Y'$ [mm-mrad] (2.2×10^5 macro-
particles) (some halo develops in vertical
plane)

Benchmark – ORBIT/ACCSIM vs. measurements

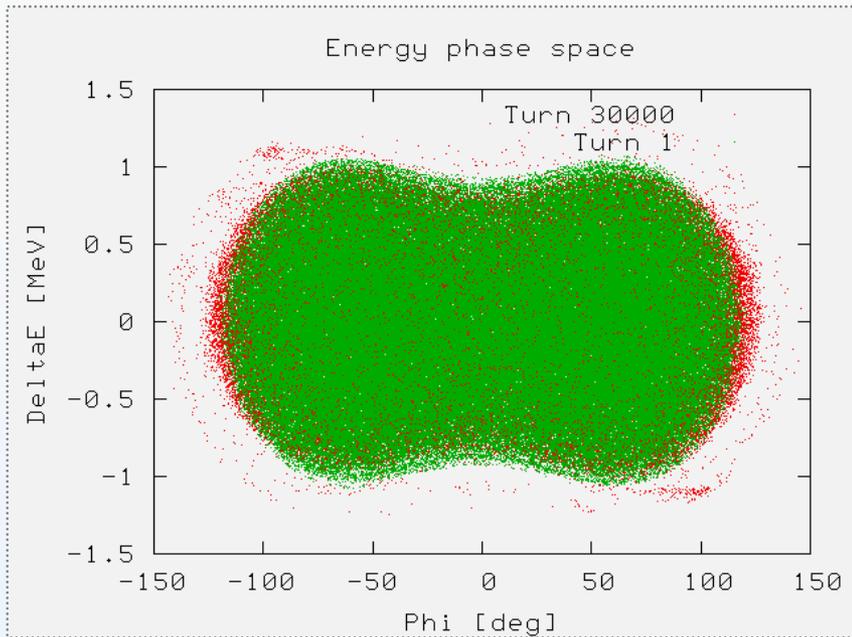
- ✓ PSB actual high-intensity beam on a 160 MeV energy plateau
 - Benchmark ORBIT & ACCSIM
 - High intensity beam ($\sim 10^{13}$ protons in one ring) on a 160 MeV energy plateau
 - Two sets of benchmark measurements were made (M. CHANEL)
 - 1. Long bunches – PSB working point $Q_{H,V}=4.21/4.35$
 - 1st & 2nd harmonic cavities at 8 kV in anti-phase
 - t=0 ms: 1.05×10^{13} p, $\varepsilon_{H,V}^n(1\sigma)=13.7/6.8$ μm , $\varepsilon_L(1\sigma)\sim 0.25$ eVs
 - t=200 ms: 1.03×10^{13} p, $\varepsilon_{H,V}^n(1\sigma)=13.1/7.5$ μm , $\varepsilon_L(1\sigma)\sim 0.25$ eVs
 - 2. Short bunches – PSB working point $Q_{H,V}=4.21/4.45^{(1)}$
 - 1st & 2nd harmonic cavities at 8 kV in phase
 - t=0 ms: 1.03×10^{13} p, $\varepsilon_{H,V}^n(1\sigma)=19.2/7.1$ μm , $\varepsilon_L(1\sigma)\sim 0.20$ eVs
 - t=200 ms: 0.96×10^{13} p, $\varepsilon_{H,V}^n(1\sigma)=20.4/7.3$ μm , $\varepsilon_L(1\sigma)\sim 0.20$ eVs
- (1) The vertical working point had to be changed to minimize the particle losses

Benchmark – ORBIT/ACCSIM vs. measurements

✓ ORBIT simulation

- 1 beam file (single injection 2×10^5 of macro-particles) holding the “steady” 6D particle distribution at 160 MeV with the right initial longitudinal/transverse emittances (PSB measurement)
- Subsequent simulation performed with space charge
- Tracking up to 3×10^4 turns
- No acceleration considered
- Parallel processing using 7 CPUs (crashes when using more CPUs!)
- Computation time ~proportional to the macro-particle numbers
 - ~1370 turns/h with 2.5×10^4 macro-particles
 - ~160 turns/h with 2×10^5 macro-particles (3×10^4 turns in ~8 days)
 - ~32 turns/h with 10^6 macro-particles? (3×10^4 turns in ~39 days?)

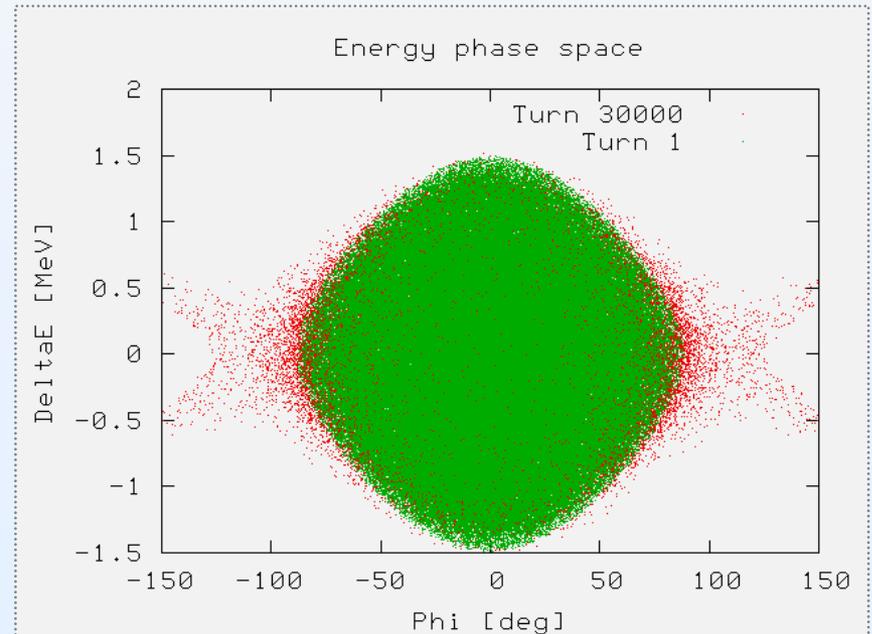
Benchmark – ORBIT/ACCSIM vs. measurements



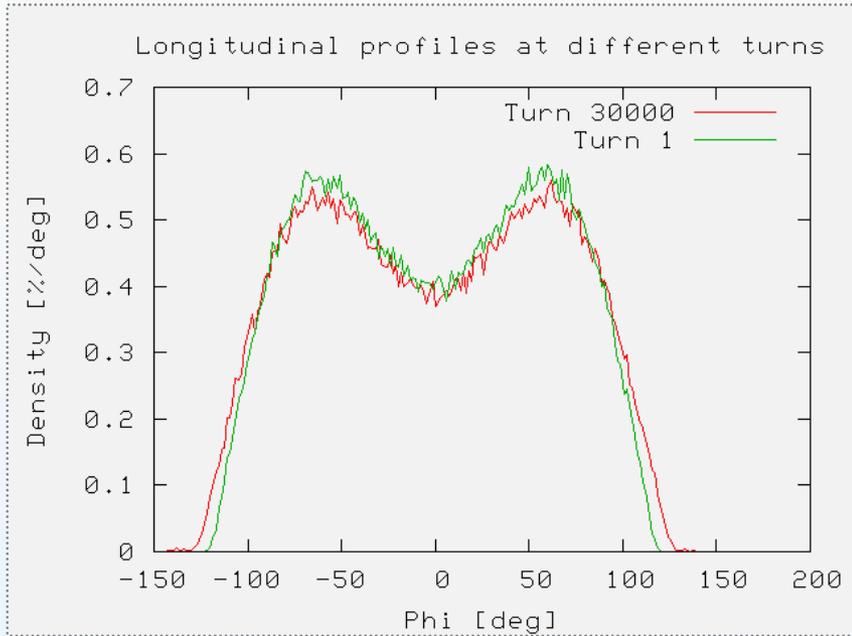
✓ ORBIT
 $Q_{H,V}=4.21/4.35$
Long bunches

Longitudinal phase-space plots
 ϕ - ΔE [deg-MeV] (2×10^5 macro-particles) (green: at turn 1, red: at turn 30000)

✓ ORBIT $Q_{H,V}=4.21/4.45$
Short bunches



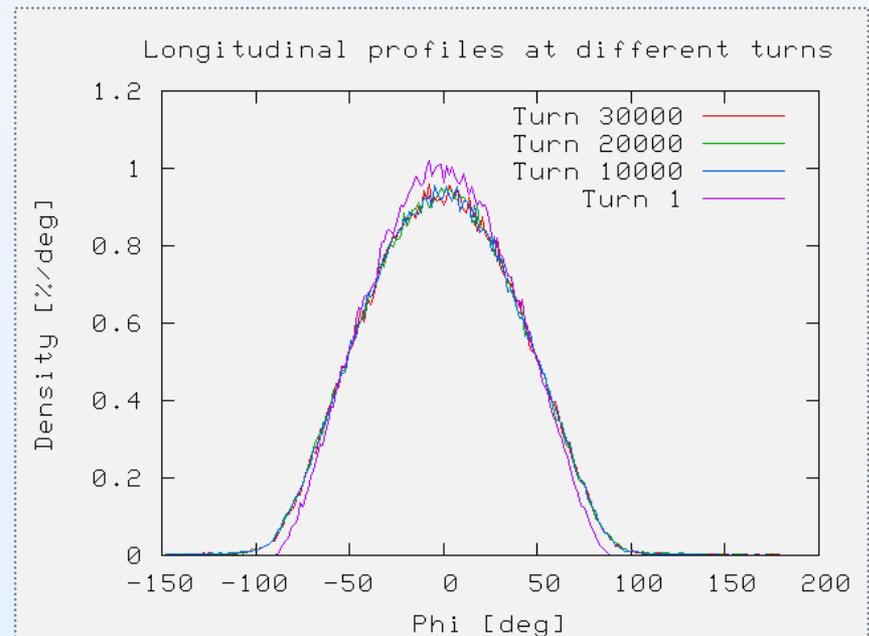
Benchmark – ORBIT/ACCSIM vs. measurements



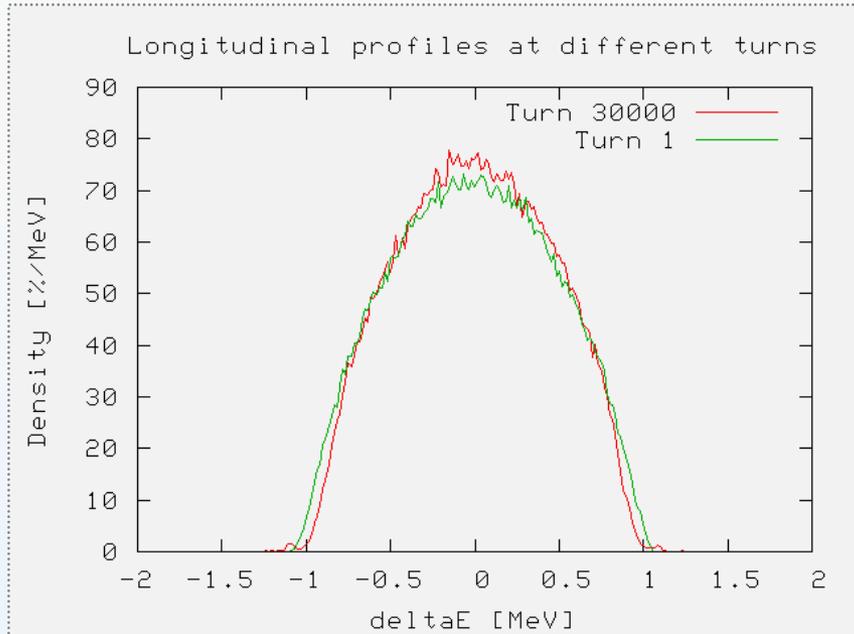
✓ ORBIT
 $Q_{H,V}=4.21/4.35$
Long bunches

Longitudinal profiles
 $\partial\text{Prob}\{\varphi\leq\phi\}/\partial\phi$ [%/deg] vs. ϕ [deg]
(φ single particle phase)
(2×10^5 macro-particles)

✓ ORBIT $Q_{H,V}=4.21/4.45$
Short bunches



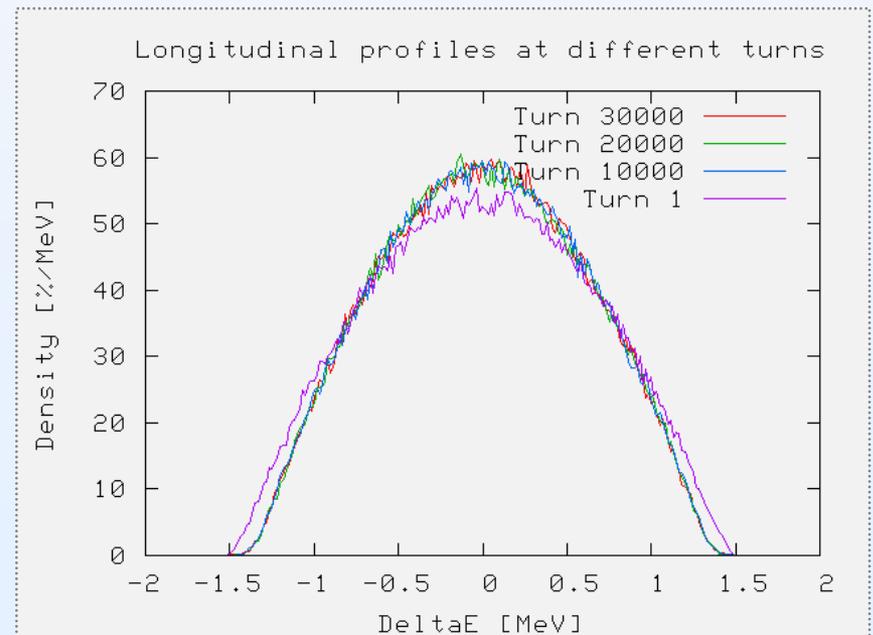
Benchmark – ORBIT/ACCSIM vs. measurements



✓ ORBIT
 $Q_{H,V}=4.21/4.35$
Long bunches

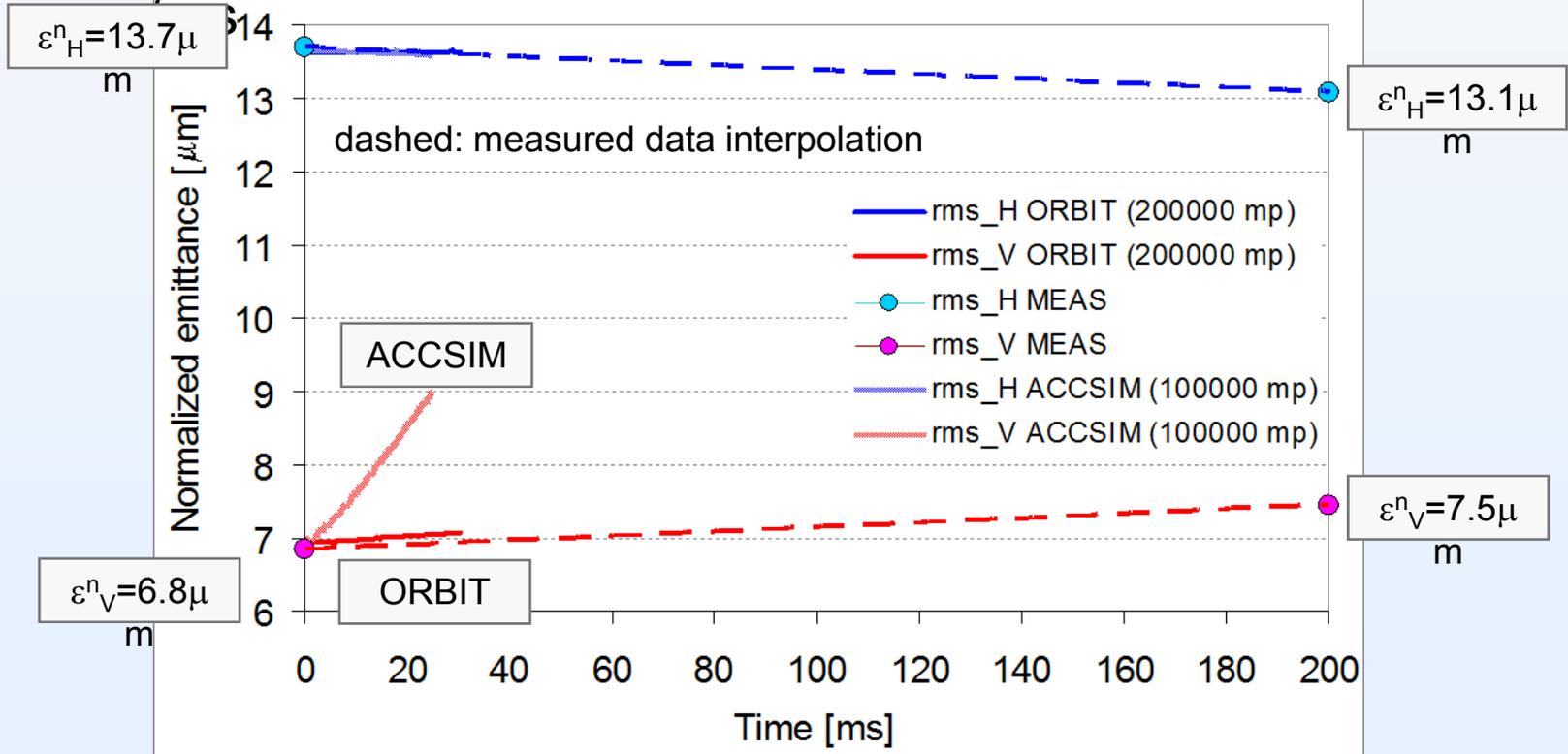
Energy distributions
 $\partial\text{Prob}\{\delta E \leq \Delta E\} / \partial \Delta E$ [%/MeV] vs. ΔE [MeV]
(δE single particle energy variation)
(2×10^5 macro-particles)

✓ ORBIT $Q_{H,V}=4.21/4.45$
Short bunches



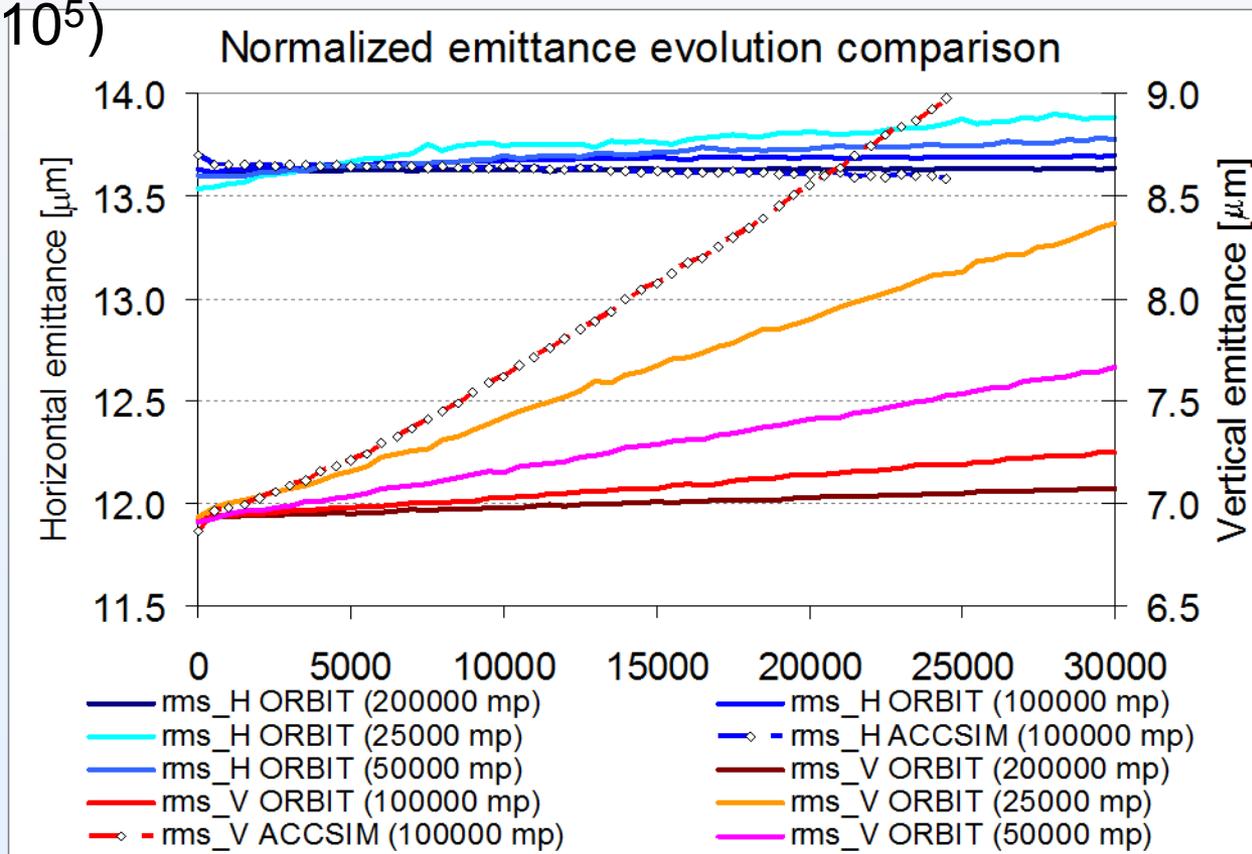
Benchmark – ORBIT/ACCSIM vs. measurements

- ✓ **ORBIT** and **ACCSIM** : Long bunches – $Q_{H,V}=4.21/4.35$
 - 2nd harmonic cavity in anti-phase
 - **ORBIT**: ~30 ms, 3×10^4 turns, $\Delta\varepsilon_{H\&V}/\Delta t \sim 5 \times 10^{-4}$ & 5×10^{-3} $\mu\text{m}/\text{ms}$
 - **ACCSIM**: ~25 ms, 2.5×10^4 turns, $\Delta\varepsilon_{H\&V}/\Delta t \sim -0.003$ & 0.1



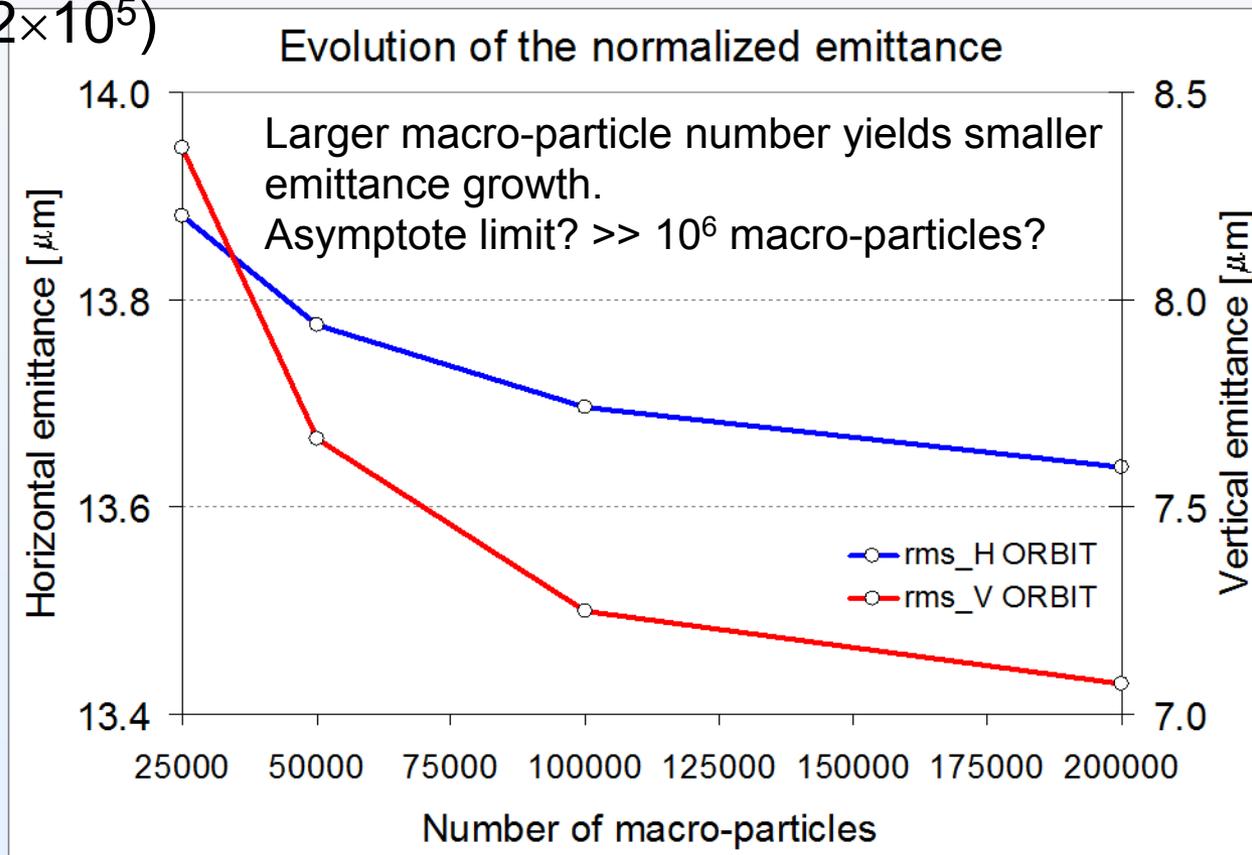
Benchmark – ORBIT/ACCSIM vs. measurements

- ✓ **ORBIT** and **ACCSIM** : Long bunches – $Q_{H,V}=4.21/4.35$
 - 2nd harmonic cavity in anti-phase
 - Transverse emittance evolution $\varepsilon_{H,V}^n(1\sigma)$ [μm] versus number of turns for various number of macro-particles (2.5×10^4 to 2×10^5)



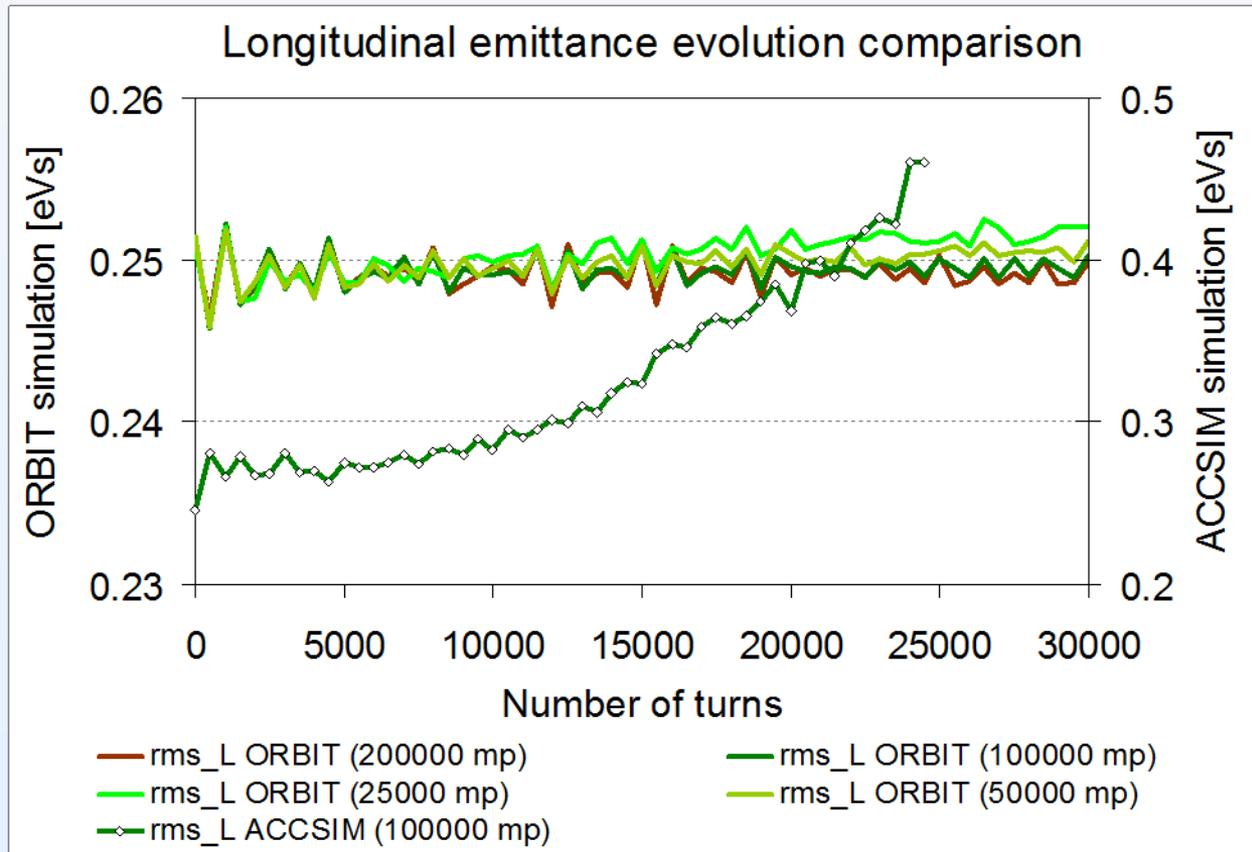
Benchmark – ORBIT/ACCSIM vs. measurements

- ✓ **ORBIT** and **ACCSIM** : Long bunches – $Q_{H,V}=4.21/4.35$
 - 2nd harmonic cavity in anti-phase
 - Transverse normalized emittance evolution $\varepsilon_{H,V}^n(1\sigma)$ [μm] (at turn 3×10^4) versus number of macro-particles (from 2.5×10^4 to 2×10^5)



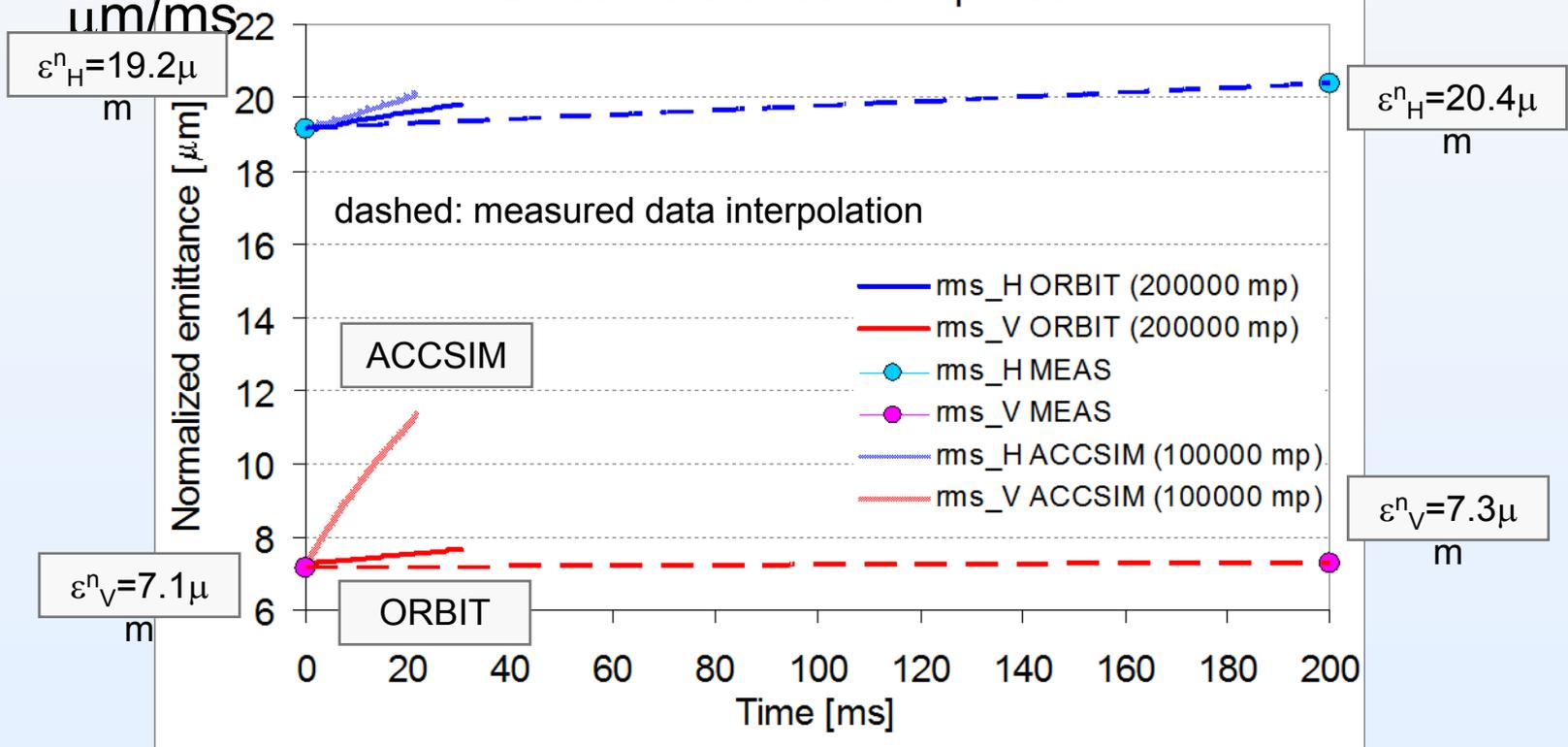
Benchmark – ORBIT/ACCSIM vs. measurements

- ✓ ORBIT and ACCSIM : Long bunches – $Q_{H,V}=4.21/4.35$
 - 2nd harmonic cavity in anti-phase
 - Longitudinal emittance evolution $\varepsilon_L^n(1\sigma)$ [eVs] for various number of macro-particles (2.5×10^4 to 2×10^5)



Benchmark – ORBIT/ACCSIM vs. measurements

- ✓ **ORBIT** and **ACCSIM** : Short bunches – $Q_{H,V}=4.21/4.45$
 - 2nd harmonic cavity in phase
 - **ORBIT**: ~30 ms, 3×10^4 turns, $\Delta\varepsilon_{H\&V}/\Delta t \sim 0.024$ & 0.013 $\mu\text{m}/\text{ms}$
 - **ACCSIM**: ~22 ms, 2.2×10^4 turns, $\Delta\varepsilon_{H\&V}/\Delta t \sim 0.04$ & 0.2 $\mu\text{m}/\text{ms}$

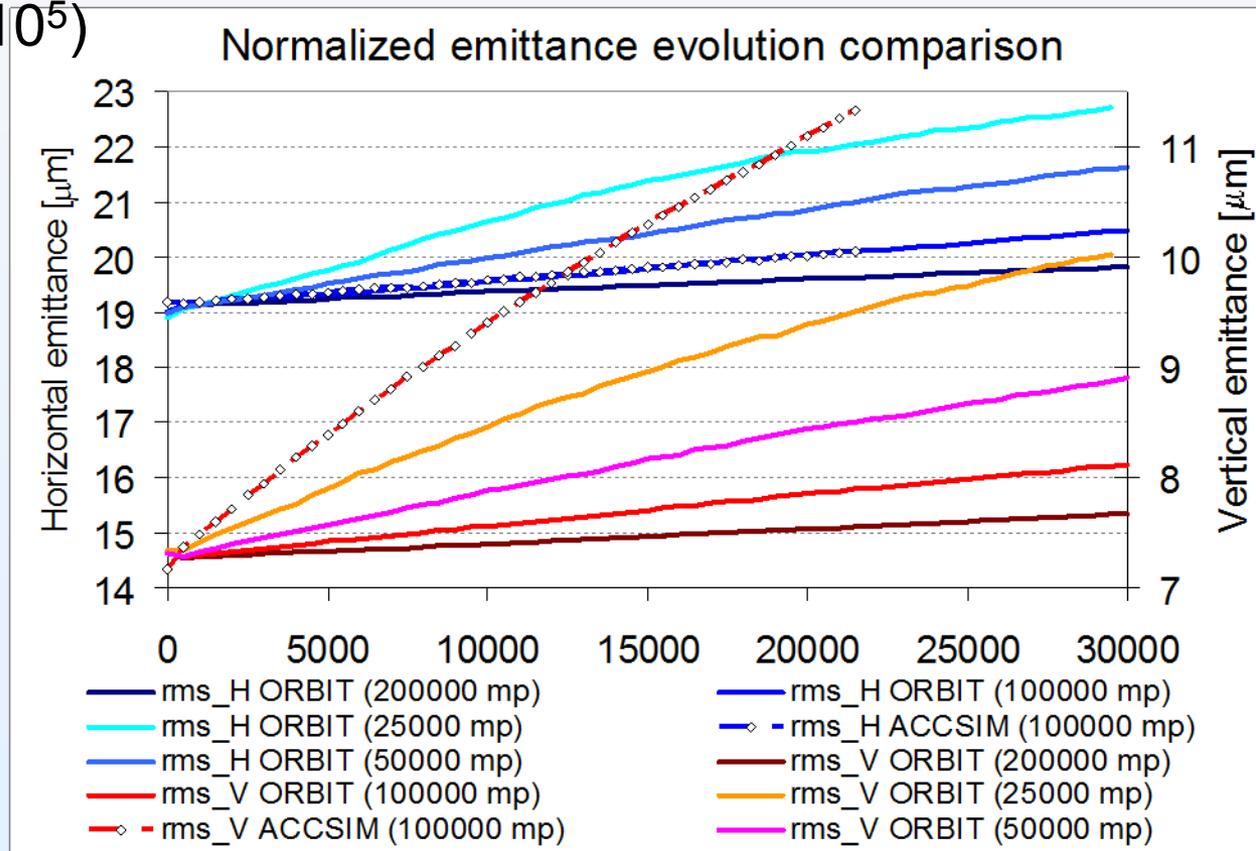


Benchmark – ORBIT/ACCSIM vs. measurements

- ✓ **ORBIT** and **ACCSIM** : Long bunches – $Q_{H,V}=4.21/4.35$
 - Only short simulation duration (time consuming)
 - **ORBIT**: Fairly good estimation of growth rates in both planes
 - **ACCSIM**: **Overestimation** / fairly good estimation of growth rates in the **vertical** / **horizontal** planes
- ✓ **ORBIT** and **ACCSIM** : Short bunches – $Q_{H,V}=4.21/4.45$
 - Only short simulation duration (computation time ~200 turns/h)
 - **ORBIT**: Slight overestimation of growth rates in both planes
 - **ACCSIM**: **Overestimation** / slight overestimation of growth rates in the **vertical** / **horizontal** planes
 - Insufficient statistics?
 - More emittance measurements set equally apart? (along the 200 ms)

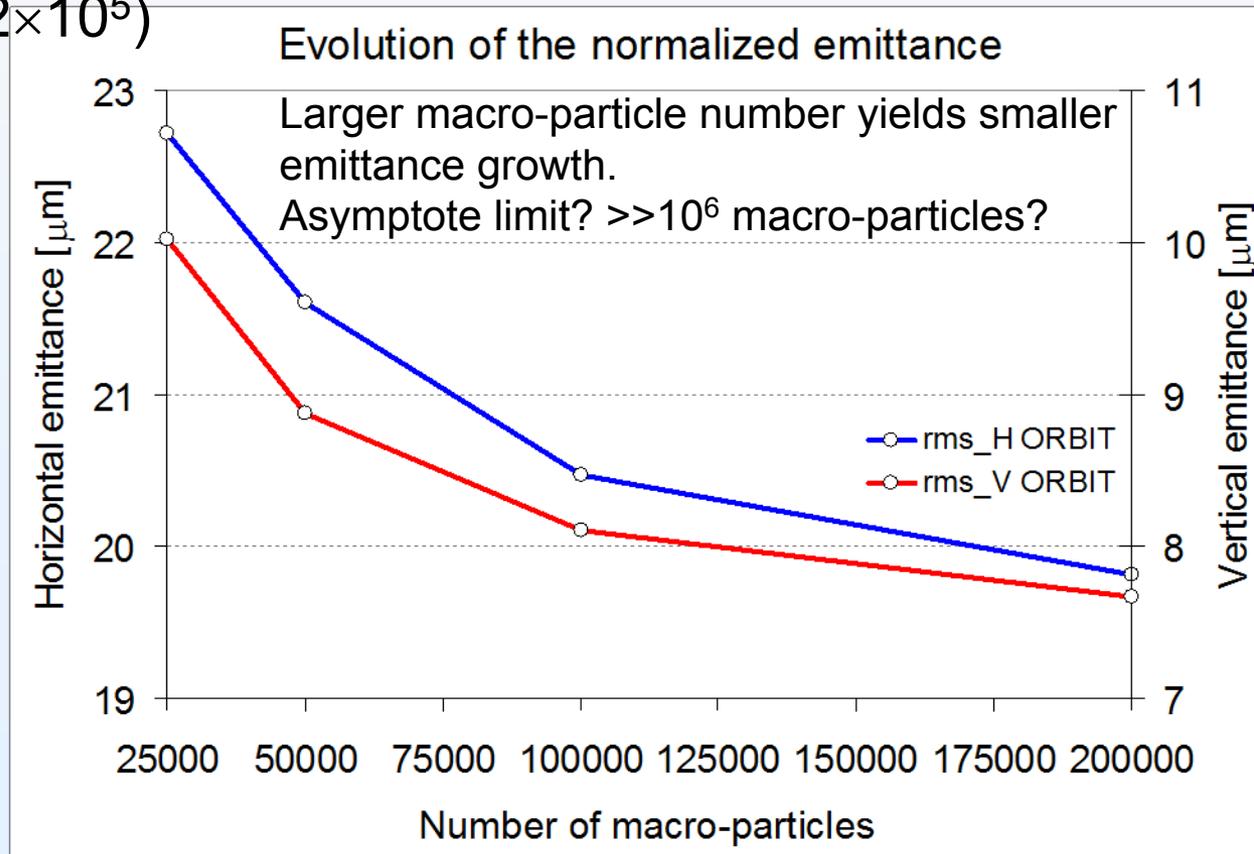
Benchmark – ORBIT/ACCSIM vs. measurements

- ✓ **ORBIT** and **ACCSIM** : Short bunches – $Q_{H,V}=4.21/4.45$
 - 2nd harmonic cavity in phase
 - Transverse emittance evolution $\varepsilon_{H,V}^n(1\sigma)$ [μm] versus number of turns for various number of macro-particles (2.5×10^4 to 2×10^5)



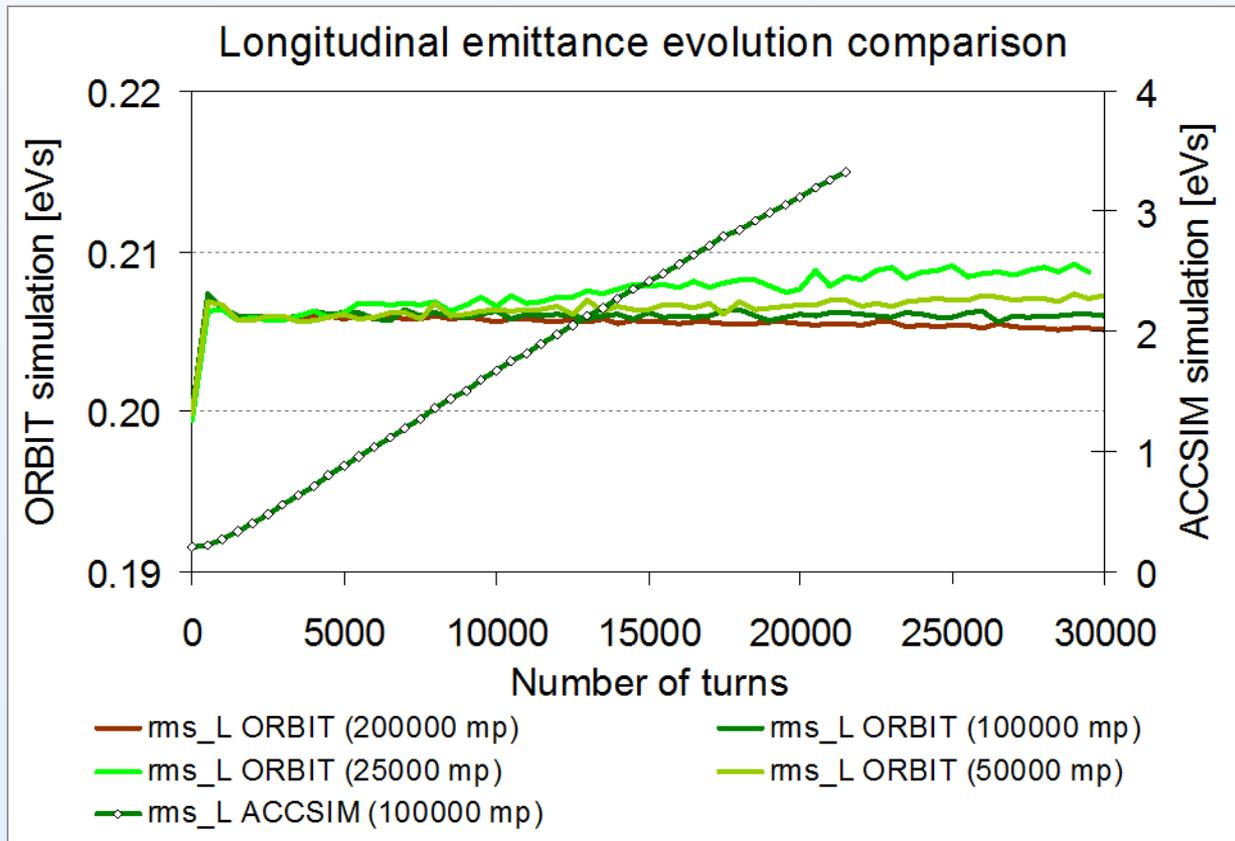
Benchmark – ORBIT/ACCSIM vs. measurements

- ✓ **ORBIT** and **ACCSIM** : Short bunches – $Q_{H,V}=4.21/4.45$
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 - Transverse normalized emittance evolution $\varepsilon_{H,V}^n(1\sigma)$ [μm] (at turn 3×10^4) versus number of macro-particles (from 2.5×10^4 to 2×10^5)

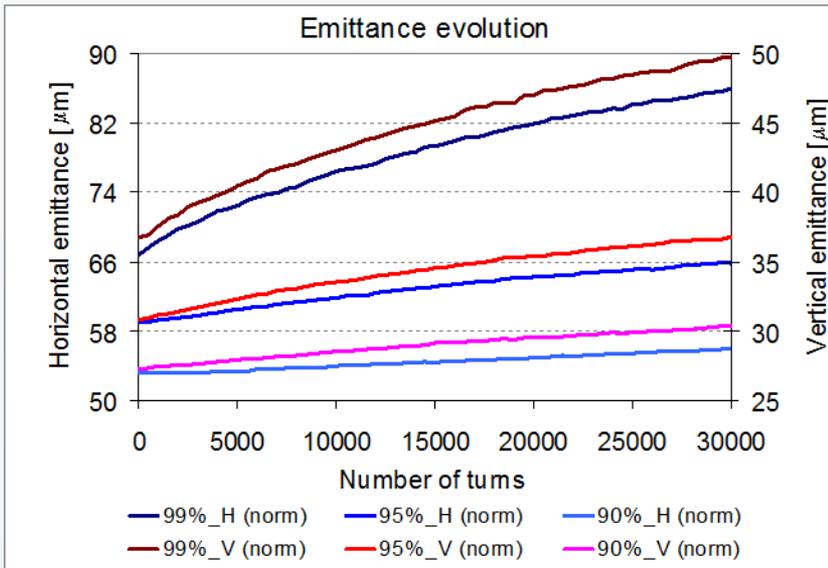


Benchmark – ORBIT/ACCSIM vs. measurements

- ✓ **ORBIT** and **ACCSIM** : Short bunches – $Q_{H,V}=4.21/4.45$
 - 2nd harmonic cavity in phase
 - Longitudinal emittance evolution $\varepsilon_L^n(1\sigma)$ [eVs] for various number of macro-particles (2.5×10^4 to 2×10^5)
 - **ACCSIM**: particles escape the bucket (initial density not quite matched)



Benchmark – ORBIT/ACCSIM vs. measurements



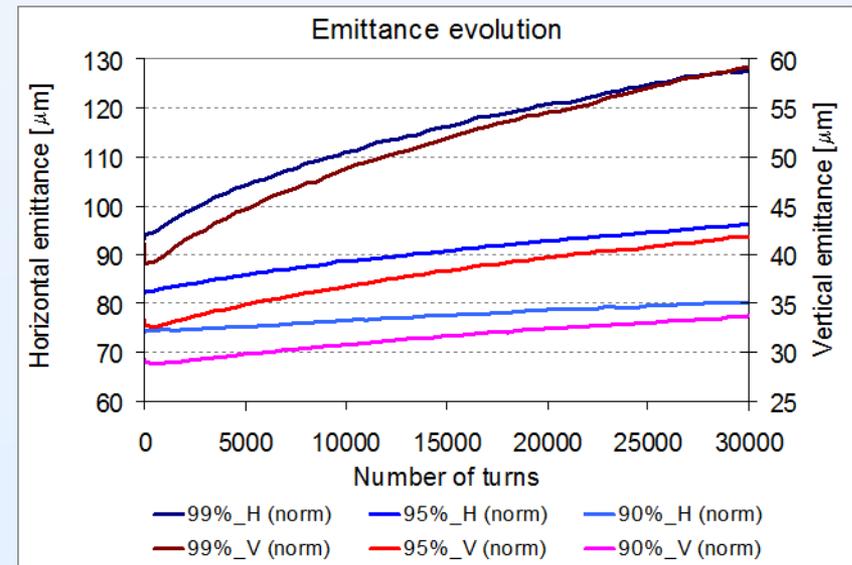
Transverse emittances

$$\varepsilon_{H,V}^n(99, 95, 90\%) [\mu\text{m}]$$

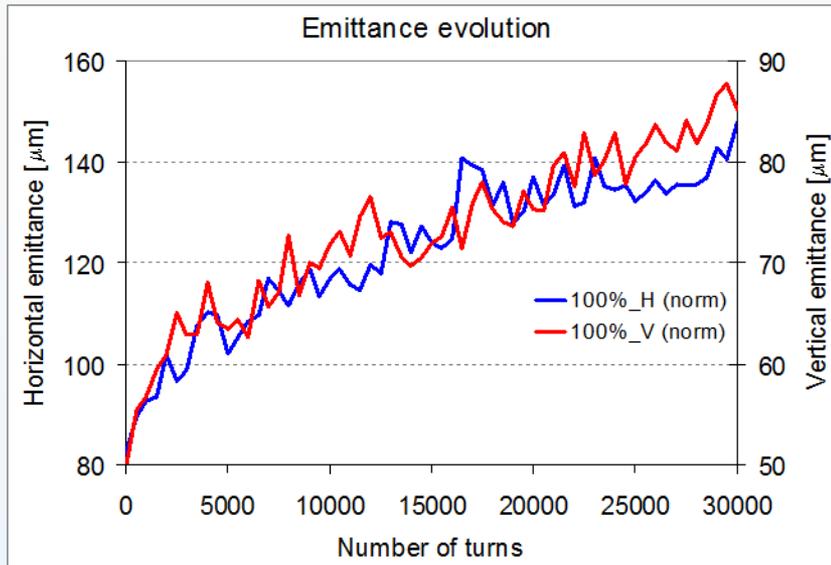
(2×10^5 macro-particles)

✓ ORBIT $Q_{H,V}=4.21/4.45$
Short bunches

✓ ORBIT
 $Q_{H,V}=4.21/4.35$
Long bunches



Benchmark – ORBIT/ACCSIM vs. measurements



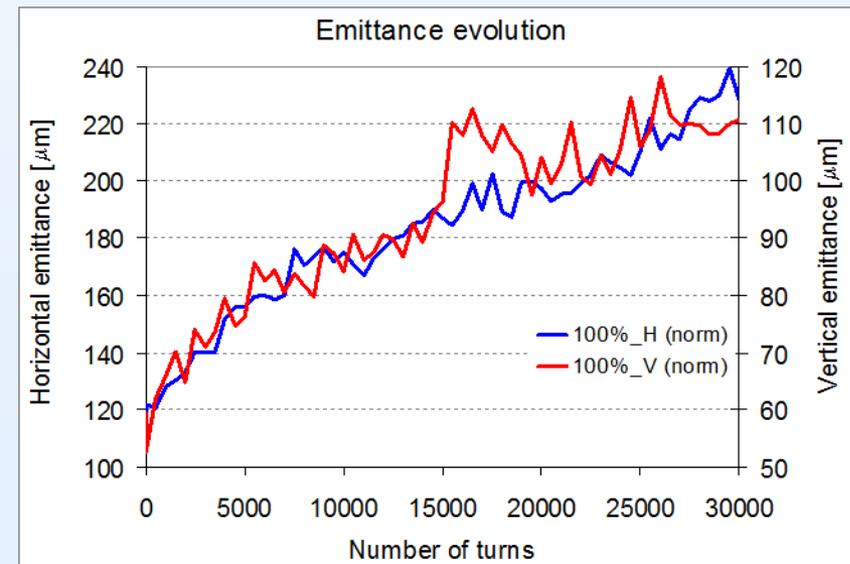
✓ ORBIT
 $Q_{H,V}=4.21/4.35$
Long bunches

Transverse emittances

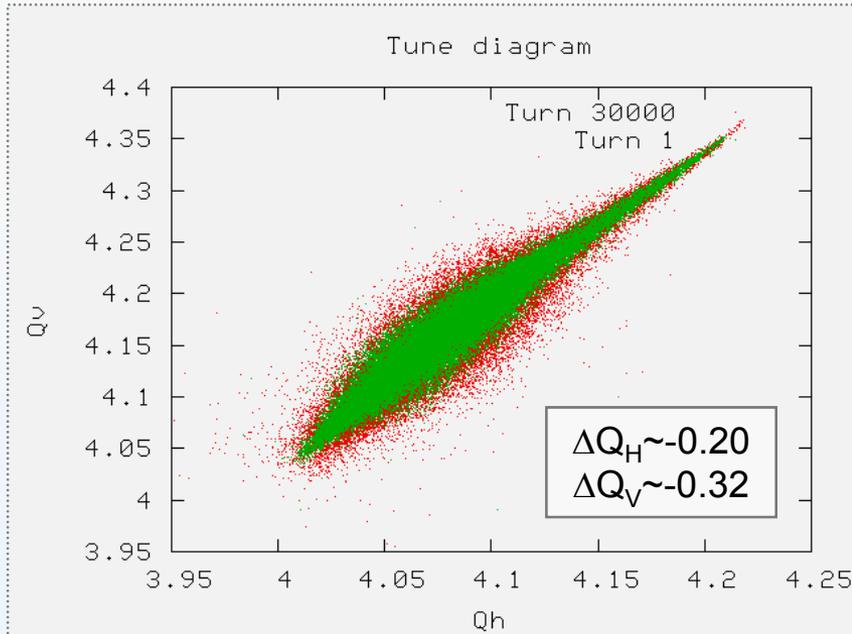
$$\varepsilon_{H,V}^n(100\%) [\mu\text{m}]$$

(2×10^5 macro-particles)

✓ ORBIT $Q_{H,V}=4.21/4.45$
Short bunches



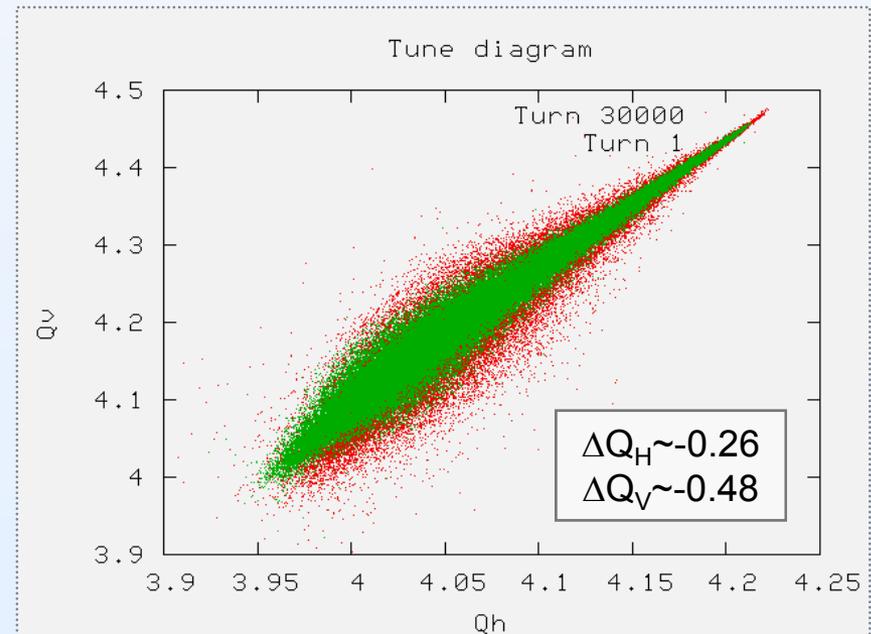
Benchmark – ORBIT/ACCSIM vs. measurements



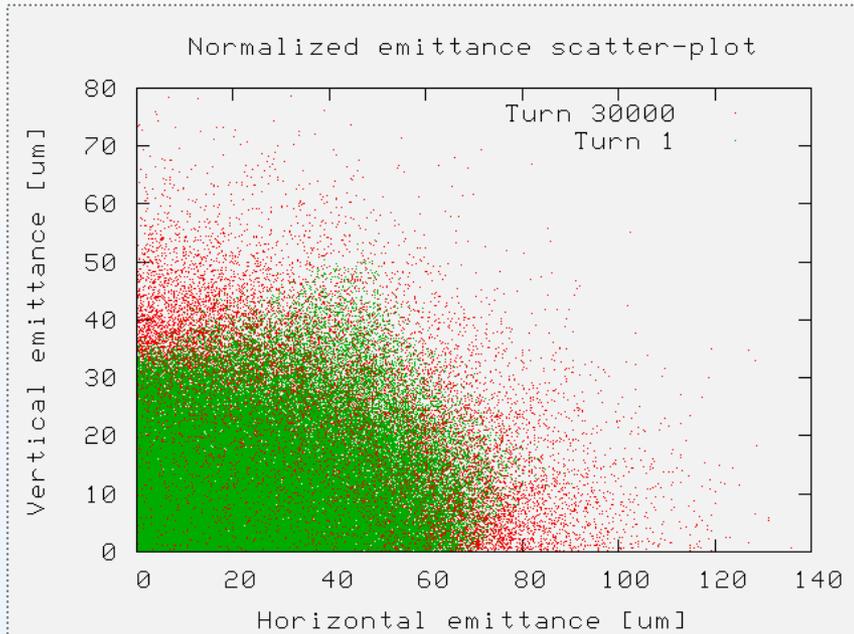
✓ ORBIT
 $Q_{H,V} = 4.21/4.35$
Long bunches

Tune diagrams
(2×10^5 macro-particles)
(green: at turn 1, red: at turn 30000)

✓ ORBIT $Q_{H,V} = 4.21/4.45$
Short bunches



Benchmark – ORBIT/ACCSIM vs. measurements



✓ ORBIT
 $Q_{H,V}=4.21/4.35$
Long bunches

Transverse emittances scatter plots $E_H^n - E_V^n$ [$\mu\text{m} - \mu\text{m}$] (2×10^5 macro-particles)

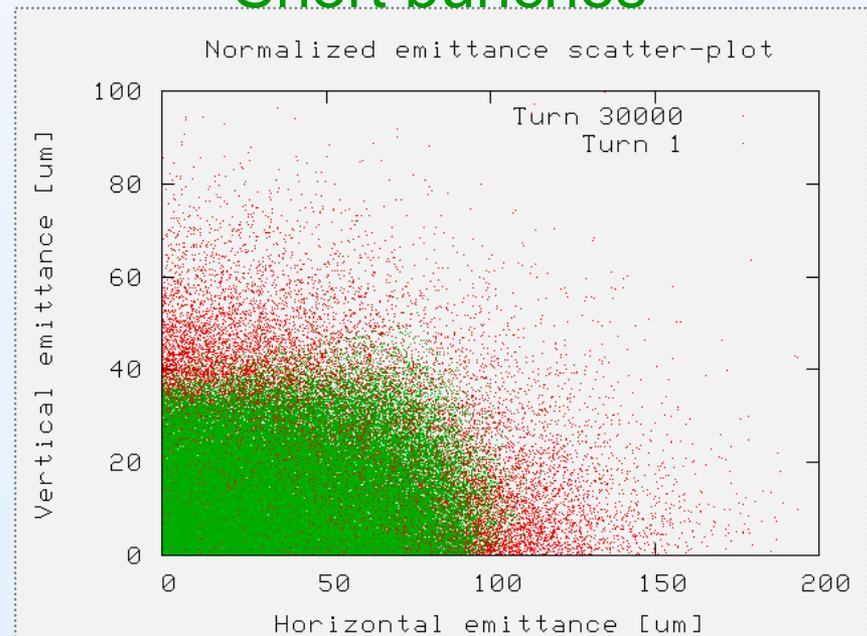
(particle emittance distribution)

($E_{H,V}^n$ single particle emittance)

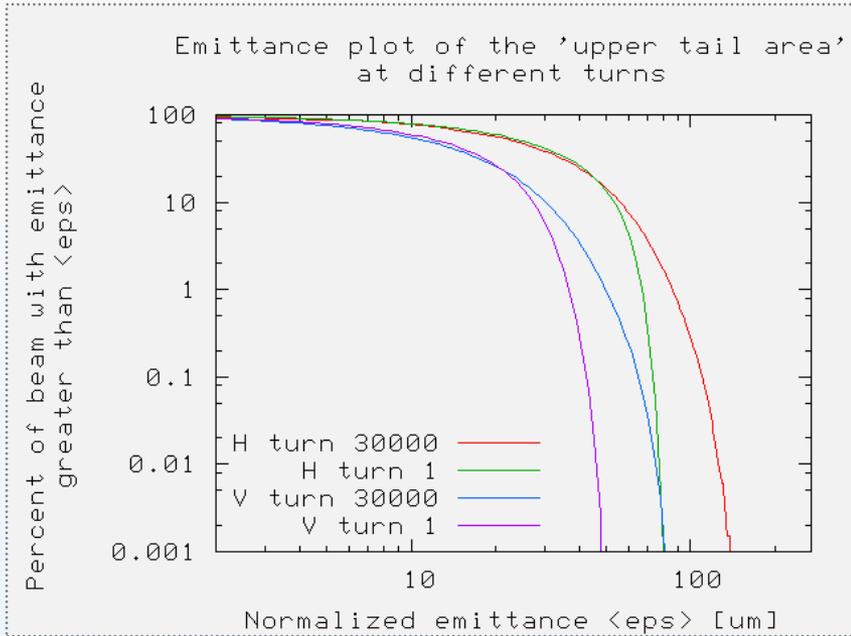
(green: at turn 1, red: at turn 30000)

✓ ORBIT $Q_{H,V}=4.21/4.45$

Short bunches



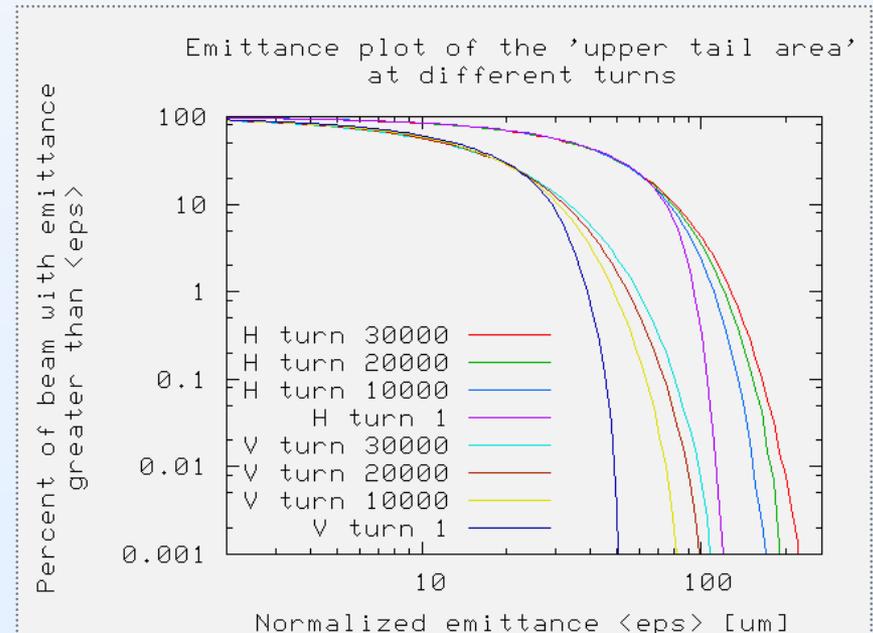
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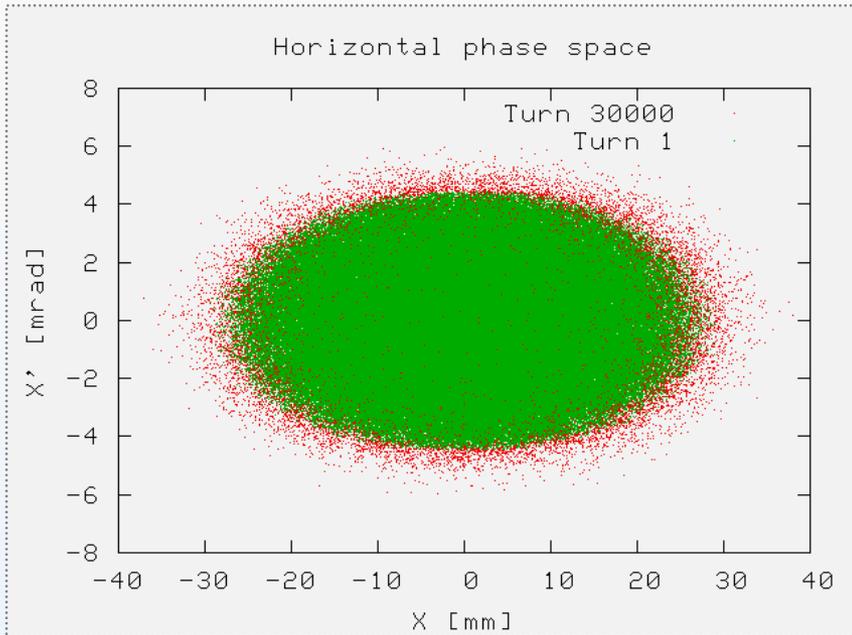
✓ ORBIT
 $Q_{H,V}=4.21/4.35$
 Long bunches

Log-log “upper tail area” plot
 $\text{Prob}\{E_{H,V}^n > \epsilon_{H,V}^n\}$ [%] vs. $\epsilon_{H,V}^n$ [μm]
 ($E_{H,V}^n$ single particle emittance)
 (2×10^5 macro-particles)

✓ ORBIT $Q_{H,V}=4.21/4.45$
 Short bunches



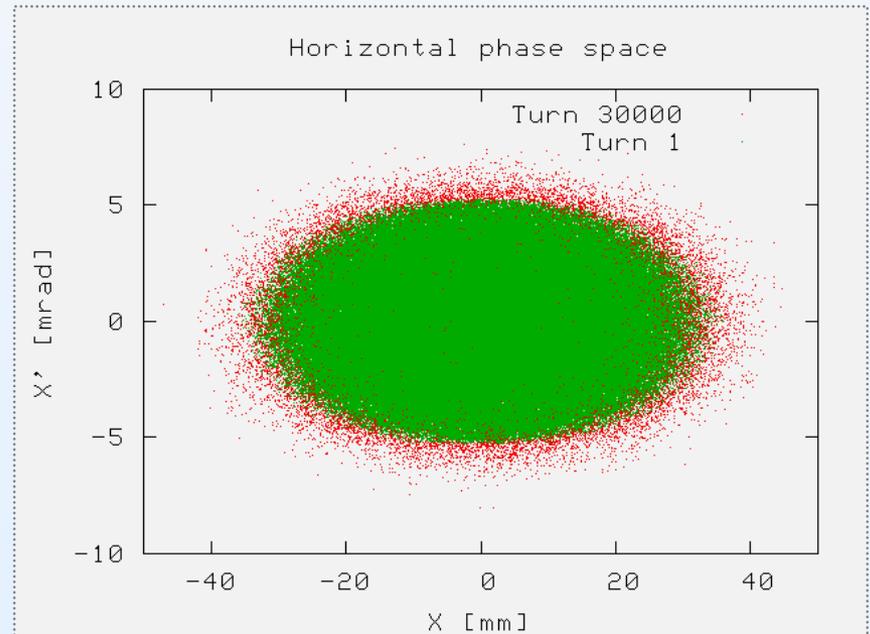
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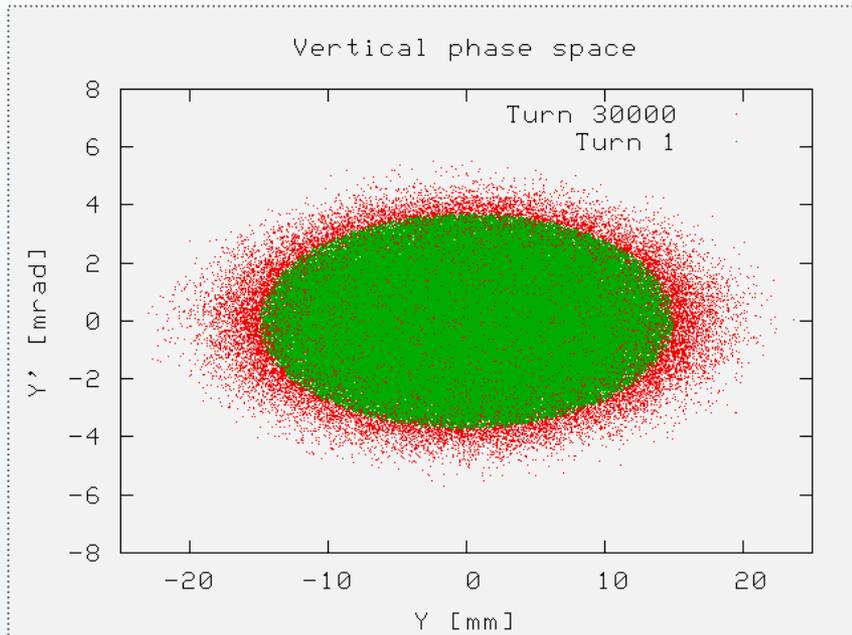
✓ ORBIT
 $Q_{H,V}=4.21/4.35$
Long bunches

Horizontal phase-space scatter plots X-X' [mm-mrad] (2×10^5 macroparticles)
(green: at turn 1, red: at turn 30000)

✓ ORBIT $Q_{H,V}=4.21/4.45$
Short bunches



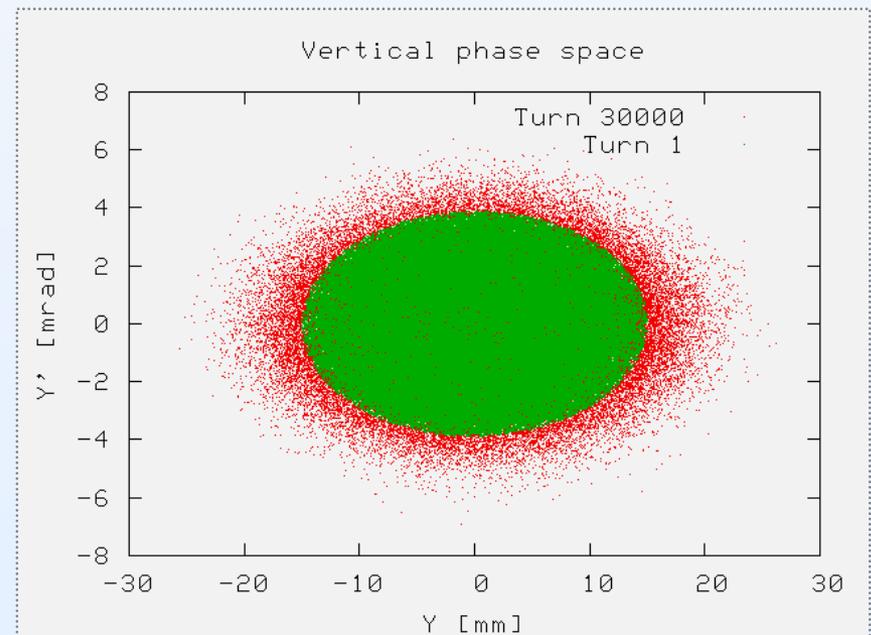
Benchmark – ORBIT/ACCSIM vs. measurements



✓ ORBIT
 $Q_{H,V}=4.21/4.35$
Long bunches

Vertical phase-space scatter plots Y-Y' [mm-mrad] (2×10^5 macro-particles)
(green: at turn 1, red: at turn 30000)

✓ ORBIT $Q_{H,V}=4.21/4.45$
Short bunches



Summary

✓ PSB injection simulations

- Controlled longitudinal injection painting scheme based on a triangular modulation of the Linac4 output energy examined
- Tailoring of the longitudinal and transverse distributions to minimize peak densities is effective in lessening the transverse emittance blow-up

✓ PSB benchmarking simulations

- Benchmark of the simulations with experiments at 160 MeV seems to indicate that the simulations done with **Orbit** are hopeful (i.e. emittance growth rates ~similar to measurements) while those conducted with **Accsim** are rather pessimistic (i.e. overestimation of growth rates but horizontal plane and long bunches)

Appendix: ORBIT/ACCSIM space charge modeling

- ✓ **ORBIT** transverse space charge routines (parallel processing)
 - 2½D space charge model (“mixed 2D & 3D models: space charge force on macro-particles scaled according to the longitudinal charge density). 3D space charge model exists too
 - Transverse space charge tracking calculation (applied at each space charge kick “nodes” inserted around the ring)
 - Pair-wise sum: “Particle-Particle” method. Computes the Coulomb force on one particle by summing the force over all other particles
 - Brute Force Particle-In-Cell (PIC): “Particle-Mesh” method. Bins the macro-particles on a grid, computes the force at each grid point and on each particle by linear interpolation from the grid (grid size automatically fitted to the beam extent)
 - FFT-PIC: Alike to the brute-force PIC but a FFT computes the force on the grid via the binned particle distribution (the fastest solver)
- ✓ **ORBIT** chromaticity (for Teapot based tracking)
 - Chromatic tune shift generated by the transfer matrix considering the $\Delta p/p$ (particle kicks at lattice elements depend on $\Delta p/p$)

Appendix: ORBIT/ACCSIM space charge modeling

- ✓ ACCSIM transverse space charge routines (non-parallel processing)
 - 2½D space charge model (similar as in ORBIT)
 - Transverse space charge tracking calculation (made at user-specified intervals in the ring)
 - Fast Multipole Method (FMM): “Particle-Particle Tree-code” method (lumping charges together). The force on each particle is derived from field calculation and kicks denoting the force integral are applied
 - Hybrid Fast Multipole (HFM): FMM is combined with elements of PIC-style methods by overlaying a proper grid on the densely-populated beam core region, assigning compound charges to the grid points, and letting FMM solve the whole system of core grid + halo charges (handle correctly large-amplitude beam halos)
- ✓ ACCSIM chromaticity (MAD8 based tracking)
 - Chromatic tune shift generated by extra particle betatron phase space rotation ($2\pi\Delta Q_{H,V}$) once or more per turn, driven by the first-order chromaticity $\xi_{H,V}$ and $\Delta p/p$